

Funk ( $m$ )

**Input** : Integer  $m$

**Output:**  $3^m - 2^m$

1 **if**  $m \leq 1$  **then**

2 | return  $m$ ;

3 **end**

4 return  $5 \times \text{Funk}(m - 1) - 6 \times \text{Funk}(m - 2)$ ;

Prove  $\text{Funk}(n)$  outputs  $3^n - 2^n$  for all  $n \geq \underline{\hspace{2cm}}$

- Base case(s): \_\_\_\_\_
- Let  $k \geq \underline{\hspace{2cm}}$ . Assume for strong induction that  $P(j)$  is true for all  $j$  such that  $\underline{\hspace{2cm}} \leq j \leq k$ .

# Draw this graph:

- $V = \{a, b, c, d, e\}$
- $E = \{\{a, b\}, \{a, c\}, \{a, d\}, \{b, c\}, \{d, e\}, \{b, e\}, \{c, e\}\}$

If

- $a =$  racoon
- $b =$  hawk
- $c =$  owl
- $d =$  squirrel
- $e =$  crow

What does the graph represent?

# Graph Applications

- Brainstorm other natural questions we might want to ask about graphs, and give a real world example where that is a useful question.